CAMTP

Center for Applied Mathematics and Theoretical Physics
Univerza v Mariboru

20. Simpozij fizikov Univerze v Mariboru

Zbornik povzetkov

hotel HABAKUK
Maribor, 14., 15. in 16. december 2023

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Urednika:	prof. dr. Marko Robnik doc. dr. Anita Prapotnik Brdnik
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Generalni pokrovitelj simpozija:

EASA - European Academy of Sciences and Arts (Salzburg)

PREDGOVOR

Naši Simpoziji fizikov Univerze v Mariboru, ali na kratko kar Božični simpoziji fizikov, imajo že neprekinjeno tradicijo od leta 2002, z izjemo obdobja korone 2020-2021, saj imamo letos že jubilejnega dvajsetega po vrsti. Namen je strokovno druženje slovenskih fizikov, ob prisotnosti ter aktivni udeležbi nekaterih uglednih kolegov iz tujine kot častnih vabljenih gostov. Letos imamo dvanajst uglednih vabljenih predavateljev iz tujine, iz odličnih raziskovalnih skupin, tako da ostajajo naša srečanja nacionalna z mednarodno udeležbo. Srečanje je le ena od številnih dejavnosti CAMTP, ki sicer organizira kar sedem serij mednarodnih znanstvenih srečanj. Glej *www.camtp.uni-mb.si*

Naše srečanje je posvečeno vsej fiziki, teoretični in eksperimentalni, pa tudi uporabni matematiki in vsem drugim temam, za katere je fizika pomembna in z njimi tesno povezana, ali pa so pomembne za fiziko.

Vsa predavanja so na ravni kolokvijev, se pravi razumljiva za splošnega fizika, in zato še posebej primerna za študente, dodiplomske in podiplomske. Takšnih splošnih srečanj na področju fizike v svetu pravzaprav skorajda ni več, čeprav so po našem prepričanju pomembna za širjenje intelektualnega obzorja vseh fizikov. Kolegi iz tujine, dosedanji udeleženci, potrjujejo to stališče in cenijo naš znanstveni program. Simpozij daje priložnost mladim raziskovalcem, da predstavijo svoje delo ter se o svojih rezultatih pogovorijo z izkušenimi znanstveniki. S to dejavnostjo prispevamo tudi k popularizaciji fizike v naši družbi, na trajen način. Menimo, da je nujno poskrbeti za večjo popularizacijo naravoslovnih ved v naši družbi, in fizika igra pri tem ključno vlogo. Vsem dodiplomskim študentom dovoljujemo brezplačno udeležbo na vseh predavanjih, in s tem prispevamo k popularizaciji fizike ter k dodatnemu izobraževanju na tem področju.

Nenazadnje bi radi poudarili, da je naše druženje pomemben prispevek pri nadaljnjih uspešnih aktivnostih Fakultete za naravoslovje in matematiko Univerze v Mariboru, ter Fakultete za matematiko in fiziko Univerze v Ljubljani, in seveda inštitutov z oddelki za fiziko, kot sta Inštitut Jožef Stefan v Ljubljani ter CAMTP v Mariboru.

V čast nam je, da je generalni pokrovitelj Simpozija Evropska akademija znanosti in umetnosti (European Academy of Sciences and Arts, Salzburg). V imenu Akademije nas bo pozdravil in nagovoril Prof. Klaus Mainzer s Tehniške Univerze v Münchnu, predsednik Akademije, ki je sicer seveda tudi vabljeni predavatelj. Sicer pa nas bo prisotnih kar 11 članov Akademije (razred IV, naravoslovne vede).

Poleg znanstvenega programa in znanstvenega druženja bomo doživeli tudi dva komorna koncerta. V četrtek 14. decembra bosta za nas igrala ugledna violončelist Nikolaj Sajko (orkester SNG Opera in balet Maribor) ter pianistka Maja Gombač (Kunstuniversität Graz), v petek 15. decembra pa mladi godalni kvartet Al Fine (Ljubljana).

ORGANIZATORJA:
Prof.Dr. Marko Robnik, član EASA, Direktor CAMTP
in Doc.Dr. Anita Prapotnik Brdnik, FGPA UM

FOREWORD

Our Symposia of Physicists at the University of Maribor, or shortly Christmas Symposia, have an uninterupted tradition since 2002, except for the corona pandemic period 2020-2021, as this year it is already the 20th one. The purpose is the scientific socializing of Slovenian physicists along with the participation of some distinguished colleagues from abroad as our honorary guests. This year we have twelve invited speakers from abroad, from some of the best research groups, so that our meetings remain national with international participation. The meeting is only one of the many activities of CAMTP - Center for Applied Mathematics and Theoretical Physics, which organizes seven series of international scientific meetings. See *www.camtp.uni-mb.si*

We would like to stress that our meeting is devoted to the entire physics, theoretical and experimental, and also applied mathematics and to all other topics, to which physics is important and closely related, or they are important for physics.

All lectures are on the level of colloquia, thus understandable for a general physicist, and therefore well suited for students, the undergraduate and graduate students. Such general meetings in the field of physics practically no longer exist in the world, although in our opinion they are important for the widening of the intellectual horizon of all physicists. Our colleagues from abroad, the participants so far, confirm our view and appreciate our scientific programme. The meeting is also an opportunity for the young researchers to present their work and discuss it with the experienced scientists. With this activity we also contribute to the promotion and the popularization of physics in our society. We are convinced that it is quite urgent to care about the more intense popularization of natural sciences in our society, and physics plays a key role in this context. All undergraduate students can attend all the lectures of the conference free of charge. In this way we contribute to the popularization of physics and the education in this field.

At the end we would like to stress that our gatherings are an important contribution to the activities of the Faculty of Natural Sciences and Mathematics (Maribor) and the Faculty of Mathematics and Physics (Ljubljana), and of course also for the institutes IJS in Ljubljana and CAMTP in Maribor.

It is our privilege that the general patron of the Symposium is the European Academy of Sciences and Arts (Salzburg). The opening address on behalf of the Academy will be delivered by Prof. Klaus Mainzer of Technical University of Munich, the President of the Academy, who also is an invited speaker. We shall be 11 members of the Academy present at the Symposium (class IV, Natural Sciences).

In addition to the scientific program and scientific socializing we shall experience two chamber music concerts. On Thursday 14 December the cellist Nikolaj Sajko (orchestra of Maribor Opera and Ballet) and pianist Maja Gombač (Kunstuniversität Graz), both well known musicians, and on Friday 15 December the young String Quartet Al Fine (Ljubljana) will perform for us.

ORGANIZERS:
Prof.Dr. Marko Robnik, Member of EASA, Director of CAMTP
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Seznam vseh udeležencev 20. Simpozija fizikov Univerze v Mariboru

List of all participants at the 20th Christmas Symposium of Physicists of the University of Maribor

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Urnik 20. Simpozija fizikov
Univerze v Mariboru

Četrtek, 14. december 2023 **Thursday, 14 December 2023**	
Chair	Robnik
09:00 – 09:15	Otvoritev/Opening
09:15 – 10:00	Mainzer
10:00 – 11:00	Skokos
11:00 – 11:30	Kava & Čaj/Coffee & Tea
11:30 – 12:30	Plessas
12:30 – 13:00	Bajc
13:00 – 13:30	Grozdanov
13:30 – 15:00	Kosilo/Lunch
Chair	Dvorak
15:00 – 15:30	Križan
15:30 – 16:00	Korpar
16:00 – 16:30	Žnidarič
16:30 – 17:00	Kava & Čaj/Coffee & Tea
17:00 – 17:30	Stöckmann
17:30 – 18:00	Marhl
19:00 – 20:00	Concert: Sajko & Gombač
20:00 – 23:00	Svečana večerja/Banquet

Petek, 15. december 2023 **Friday, 15 December 2023**	
Chair	Grozdanov
09:00 – 09:30	Casati
09:30 – 10:30	Prosen
10:30 – 11:00	Bonča
11:00 – 11:30	Kava & Čaj/Coffee & Tea
11:30 – 12:00	Vidmar
12:00 – 12:30	Jiaozi Wang
12:30 – 13:00	Gosak
13:00 – 13:30	Biro
13:30 – 15:00	Kosilo/Lunch
Chair	Stöckmann
15:00 – 15:30	Robnik
15:30 – 16:00	Qian Wang
16:00 – 16:30	Yan
16:30 – 17:00	Kava & Čaj/Coffee & Tea
17:00 – 17:30	Šarler
17:30 – 18:00	Cvetič
18:00 – 18:30	Zwitter
19:00 – 20:00	Concert: Al Fine
20:00 – 23:00	Svečana večerja/Banquet

Sobota, 16. december 2023 **Saturday, 16 December 2023**	
Chair	Prosen
09:00 – 09:30	Burgdörfer
09:30 – 10:00	Schmelcher
10:00 – 10:30	Dvorak
10:30 – 11:00	Wilkinson
11:00 – 11:30	Kava & Čaj/Coffee & Tea
11:30 – 12:00	Paletta
12:00 – 12:30	Čopar
12:30 – 12:45	Marinko
12:45 – 15:00	Lunch
Chair	Plessas
15:00 – 15:30	Vogrin
15:30 – 16:00	Romanovski
16:00 – 16:30	Ferčec
16:30 – 17:00	Kava & Čaj/Coffee & Tea
17:00 – 17:30	Huang
17:30 – 18:00	Mahdi
19:00 – 22:00	Večerja/Dinner

Heunova enačba in kvazinormalen spekter

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Heunova enačba je navadna diferencijalna enačba drugega reda s štirimi regularnimi singularnostmi. Med drugim jo rešujemo pri opisu črnih lukenj v asimptotskih dS/AdS prostorih. Pred kratkim so zapisali [1] eksakten analitičen izraz za termičen propagator v konformni teoriji polja preko dualnosti AdS/CFT z uporabo znane tehnike [2] za rešitev Heunove enačbe. V tem seminarju bom najprej podal kratek uvod v Heunovo enačbo, nato pa pokazal kako se račun občutno poenostavi pri iskanju kvazinormalnega spektra [3].

Reference

[1] G. Bonelli, C. Iossa, D. Panea Lichtig in A. Tanzini, *Commun. Math. Phys.* **397** (1997) (2023) no.2, 635-727.

[2] M. Dodelson, A. Grassi, C. Iossa, D. Panea Lichtig in A. Zhiboedov, *SciPost Phys.* **14** (2023) no.5, 116.

[3] B. Bajc, O. Lisovyy in S. Grozdanov, v pripravi.

The Heun equation and quasinormal modes

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The Heun equation is an ordinary differential equation of second order with four regular singularities. It appears among others in the description of black holes in asymptotically dS/AdS spacetimes. Recently an exact analytic closed form for the thermal CFT propagator has been written down [1] via the AdS/CFT correspon- dence using a known technique [2] for solving the Heun equation. In this talk I will give a short introduction into the Heun equation and show how can one simplify considerably the computation of the quasinormal modes [3].

References

[1] G. Bonelli, C. Iossa, D. Panea Lichtig and A. Tanzini, *Commun. Math. Phys.* **397** (1997) (2023) no.2, 635-727.

[2] M. Dodelson, A. Grassi, C. Iossa, D. Panea Lichtig and A. Zhiboedov, *SciPost Phys.* **14** (2023) no.5, 116.

[3] B. Bajc, O. Lisovyy and S. Grozdanov, in preparation.

Hirsch-index scaling and limits from gintropy

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It is shown that the Hirsch index, used in evaluating citation popularity of individual scientists and institutions, is proportional to the gintropy (an entropy like quantity derived from the Gini index, characterizing income inequalities by a single number) in case of a Tsallis – Pareto distribution. Several scaling assumptions follow from this, as well as limits from the maximum of gintropy. These analytical results are compared to massive data from google scholar, collecting publication and citation numbers together with the Hirsch index. Earlier linear assumptions, seen in some data, appear with a validity limited to low and medium Hirsch indices.

References

[1] T.S. Biró, A. Telcs, M. Józsa and Z. Néda: Gintropic scaling of scientometric indexes, *Physica A: Statistical Mechanics and Its Applications* **618** (2023) 128717.

[2] T.S. Biró, A. Telcs, M. Józsa, Z. Néda: f-Gintropy: an Entropic Divergence Ranking based on the Gini Index, *Entropy* **24** (2022) 407.

[3] T.S. Biró, Z. Néda: Gintropy: A Gini Index Based Generalization of Entropy, *Entropy* **22** (2020) 879.

Optična manipulacija bipolaronov v sistemu z nelinearno elektronsko-fononsko sklopitvijo

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Predstavil bom kvantno mehansko evolucijo dveh elektronov, ki sta nelinearno sklopljena s kvantnimi fononi. Analiziral bom dinamični odziv sistema, ki je podvržen kratkemu prostorsko enakomernemu optičnemu impulzu, ki se sklaplja z vibracijskimi načini. Nelinearna elektronsko fononska sklopitev lahko zmehča ali okrepi fononsko frekvenco v prisotnosti elektronske gostote. V prvem primeru zunanji optični impulz, s frekvenco, ki je tik pod fononsko frekvenco, generira privlačno sklopitev med elektroni in vodi v dolgoživo vezano stanje tudi po tem, ko je optični impulz izklopljen. Privlačna sklopitev izvira iz dinamične modifikacije fononske porazdelitve, ki inducira metastabilno stanje. S povečanjem frekvence impulza se privlačna elektron-elektronska interakcija spremeni v odbojno. Dva zaporedna optična impulza z različnimi frekvencami lahko preklapljata med privlačno in odbojno interakcijo. Nazadnje pokažem, da je impulzno inducirana vezava elektronov učinkovita tudi za šibko disperzivne optične fonone, v prisotnosti anharmoničnega fononskega spektra in v dveh dimenzijah.

Reference

[1] K. Kovač, D. Golež, M. Mierzejewski, and J. Bonča, arXiv:2305.09238

Optical manipulation of bipolarons in a system with nonlinear electron-phonon coupling

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I will present full quantum mechanical evolution of two electrons nonlinearly coupled to quantum phonons and simulate the dynamical response of the system subject to a short spatially uniform optical pulse that couples to dipole-active vibrational modes. Nonlinear electron-phonon coupling can either soften or stiffen the phonon frequency in the presence of electron density. In the former case, an external optical pulse tuned just below the phonon frequency generates attraction between electrons and leads to a long-lived bound state even after the optical pulse is switched off. It originates from a dynamical modification of the self-trapping potential that induces a metastable state. By increasing the pulse frequency, the attractive electron-electron interaction changes to repulsive. Two sequential optical pulses with different frequencies can switch between attractive and repulsive interaction. Finally, we show that the pulse-induced binding of electrons is shown to be efficient also for weakly dispersive optical phonons, in the presence anharmonic phonon spectrum and in two dimensions.

References

[1] K. Kovač, D. Golež, M. Mierzejewski, and J. Bonča, arXiv:2305.09238

Attosecond Chronoscopy: From Atoms to Condensed Matter

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Observing and clocking non-equilibrium electronic dynamics in real time has developed into one of the key areas of attosecond physics [1, 2]. Attosecond chronoscopy holds the promise to provide novel information on many-electron systems complementary to conventional spectroscopy. The timing of the photoelectric effect represents one of the first breakthroughs of attosecond chronoscopy [3, 4]. Its extension to condensed matter opens up new opportunities to explore electronic band structures and topology, electron transport, and decoherence. We will illustrate the timing of electronic processes with the help of a few recent prototypical examples. They include the Eisenbud-Wigner-Smith (EWS) and transport time delay in layered materials [5, 6], the influence of the collective screening response on electron timing, the quest for identifying the speed limit of optoelectronics [7], timing of valleytronics in graphene [8], and first results on time-resolved non-linear atom-radiation interactions [9].

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[1] M. Hentschel et al., Nature 414, 509, (2001).
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[3] R. Pazourek, S. Nagele, J. Burgdörfer, Rev. Mod. Phys. 87, 765, (2015).
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[8] T. Fabian et al., Phys. Rev. B. 106, 125419 (2022).
[9] W. Jiang et al., submitted to PRL (2023).

Quantum classical correspondence and finite-time dynamics

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According to Max Jammer: "In fact, there was rarely in the history of physics a comprehensive theory which owed so much to one principle as quantum mechanics owed to Bohr's correspondence principle". In particular, in the field of quantum chaos, integrable or chaotic classical dynamics is associated to Poisson or Wigner- Dyson distribution, respectively. However this correspondence fails in typical situations e.g. in presence of dynamical localization, for systems with divided phase space and for pseudo integrable systems. This failure is at the origin, for example, of conflicting results for polygonal billiards. By considering a correspondence between classical finite-time trajectories and the eigenfunctions and eigenvalues in an energy shell we provide a criterium to extend the classical quantum correspondence to all regimes of classical motion. Our criterium remains valid in the deep quantum regime.

Reference

[1] M. Jammer, *The conceptual developments of quantum mechanics* (McGraw-Hill New York, 1966).

[2] Zhen-Qi Chen, Rui-Hua Ni, Ya-Lei Song, Liang Huang, Jiao Wang, and Giulio Casati, Preprint

Modeli in realizacije dvodimenzionalnega nematika

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Nematski tekoči kristali imajo v idealizaciji na dve dimenziji strukturo, ki omogoča poenostavljeno matematično obravnavo. Polarni kot nematskega direktorja zadosti Laplaceovi enačbi, kar pomeni, da lahko tako direktor kot njegov polarni kot modeliramo kot kompleksno analitično funkcijo [1,2]. V tem pogledu so defekti ničle in poli analitične funkcije, večličnost vektorske reprezentacije direktorskega polja pa se ujema z večličnostjo korenskih funkcij.

Predstavil bom značilnosti kompleksnega opisa in posplošitev ovojnega števila defektov na kompleksne vrednosti, ter algoritem, ki omogoča določanje direktorskega polja v okolici poljubnega števila majhnih delcev z različnimi robnimi pogoji [3,4].

Nazadnje bom prikazal uporabo algoritma za opis eksperimentalnih rezultatov nematika v tanki plasti ob prisotnosti mikro stebričkov.

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Models and realizations of two-dimensional nematics

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In two-dimensional idealization, nematic liquid crystals have a structure that allows simplified mathematical modeling. The polar angle of the nematic director satisfies the Laplace equation, meaning that both the director and the polar angle can be represented by a complex analytical function [1,2]. In this representation, defects are zeroes and poles of the function, and the multivalued nature of the director field corresponds to the multivaluedness of the square root function.

I will present the features of the complex representation, a generalization of the winding number of defects to complex values, and an algorithm allowing calculation of the director field around an arbitrary set of small particles with various boundary conditions [3,4].

Finally, I will demonstrate the use of this algorithm to describe the experimental results of a thin nematic layer in the matrix of microposts.

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Geometrični izvor višjih simetrij v kvantni teoriji polja

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S preučevanjem teorije strun na singularnih nekompaktnih prostorih X s postopkom rezanja in lepljenja singularnosti, ki segajo do meje X, lahko pokažemo pojav simetrij višje oblike v nastalih kvantnih teorijah polja. Proučili bomo usodo teh simetrij, ko postanejo prostori X kompaktni z nadaljnjo uporabo tehnik lepljenja. Poudarili bomo konstrukcije, ko so prostori X eliptično vlaknasti Calabi-Yaujevi mnogoterniki, ki ustrezajo F-teoriji, geometrijskemu režimu teorije strun in vključujejo nastali kvant teorije polja standardnega modela. Tam lahko te rezultate primerjamo s prejšnjimi študijami, kodiranimi v aritmetični strukturi eliptičnih krivulj, gradnikov eliptično vlaknatih prostorov.

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Geometric Origin of Higher Symmetries in Quantum Field Theory

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By studying String Theory on singular non-compact spaces X we demonstrate, via a process of cutting and gluing of singularities that extend to the boundary of X, the appearance of higher-form symmetries in the resulting quantum field theories. We study the fate of these symmetries when spaces X become compact by further employing gluing techniques. We highlight constructions when spaces X are elliptically fibered Calabi-Yau manifolds, which correspond to F-theory, the geometric regime of String Theory, and include resulting quantum field theories of the Standard Model. There we can compare these results to previous studies, encoded in the arithmetic structure of elliptic curves, the building blocks of elliptically fibered spaces.

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Could there be a Fifth Giant Planet in the Solar Sytem?

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It is known from several investigations that our planetary system as it is with 8 planets and many other smaller bodies like asteroids, comets will be stable for billions of years. For the moment we ignore the 4 terrestrial planets and concentrate on the Gas Giants Jupiter, Saturn, Uranus an Neptune. What's about another Gas Giant present in the early Solar System - a question which was posed in several papers e.g. Nesvorny and Morbidell (2012). They studied the dynamics of a hypothetical early planetary system consisting of 5 and even 6 giant planets! It turned out that of special interest is to deal with a fifth large planet. In this system in some of the many thousands numerical integrations one planet was ejected and the planetary system survive as a stable one consisting of four planets. In our numerical simulation we asked the question whether there could survive an additional giant planet like Uranus between Jupiter and Saturn on a stable orbit. Our results show in extension of older papers Dvorak and Kubala (2022) and Dvorak and Cuntz (2023) that on special initial semi-major axes between a=7.12 and a=7.28 such a fictive body could survive for up to 0.6 Gigayears which is 10 percent of the estimated life-time of our Solar System. We show in a series of graphs the respective results and dicuss them.

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Limitni cikli v sistemih NDE

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Najprej bom razložila Hopfovo bifurkacijo za ravninske sisteme. Opisala bom limitne cikle na centralni mnogoterosti in degenerirane Hopfove (Bautinove) bifurkacije. Nato bom predstavila enega izmed najbolj znanih problemov kvalitativne teorije navadnih diferencialnih enačb - Hilbertov 16. problem o številu limitnih ciklov dvo-dimenzionalnih sistemov

$$\dot{x} = P_n(x, y), \quad \dot{y} = Q_n(x, y)$$

(n je maksimalna stopnja polinomov na desni strani sistema). Bistven del problema je problem ocenitve maksimalnega število limitnih ciklov, ki bifurcirajo iz singularne točke tipa center ali fokus pod vplivom majhnih motenj koeficientov sistema, t.j. problem cikličnosti. Ključna značilnost našega pristopa je, da je v primeru elementarne singularne točke problem cikličnosti reduciran na algebraični problem iskanja baze določenega polinomskega ideala. Ta pristop nato uporabimo za problem cikličnosti poddružine kubičnih sistemov.

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Limit cycles in systems of ODE's

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First, I will discuss a Hopf bifurcation for planar systems. I will describe also limit cycles on the center manifold and degenerate Hopf (Bautin) bifurcations. Then, I will present one of the most famous problems in qualitative theory of ordinary differential equations - Hilbert's sixteenth problem on the number of limit cycles of two dimensional polynomial systems

$$\dot{x} = P_n(x, y), \quad \dot{y} = Q_n(x, y)$$

(n is the maximum degree of the polynomials on the right-hand side of the system). An essential part of the problem is the problem of estimating of the maximum number of limit cycles which can bifurcate from a singular point of center or focus type under small perturbations of coefficients of the system, the so-called cyclicity problem. The key feature of our approach is that in the case of an elementary singular point the problem of cyclicity is reduced to the algebraic problem of searching for a basis of a certain polynomial ideal. We apply this approach for solving the cyclicity problem for a subfamily of cubic systems.

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Preučevanje zapletenosti dinamike v omrežjih celic beta: nauki iz fenomenoloških modelov

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Fenomenološki modeli igrajo ključno vlogo pri preučevanju kompleksnih bioloških sistemov. Z zagotavljanjem poenostavljene, vendar natančne predstavitve realnih pojavov služijo kot most med podrobnostmi bioloških sistemov in našim razumevanjem njihovih osnovnih principov. Ta abstrakcija nam omogoča izluščiti temeljne uvide, razkriti osnovne mehanizme ter olajšati globje razumevanje dinamike sistema. Poleg tega poenostavlja interpretacijo eksperimentalnih podatkov, kar omogoča prepoznavanje organizacijskih principov in vzorcev delovanja. V tem prispevku bom predstavil, kako se lahko fenomenološki modeli uporabljajo za preučevanje zapletenosti dinamike v omrežjih celic beta. V teh večceličnih enotah več sto celic beta, ki delujejo sinhrono in proizvajajo sekretorne pulze inzulina, hormona ključnega za nadzor presnovne homeostaze. Njihovo kolektivno ritmično aktivnost omogoča medcelična sklopitev, zanjo pa je značilna multimodalnost, ki izvira iz prepleta povratnih zank med različnimi podsistemi. Na naravo kolektivne aktivnosti vpliva tudi njihova funkcionalna heterogenost. Iz teh razlogov je večcelična dinamika populacij celic beta zelo kompleksna. Z uporabo fenomenološkega modela bom najprej pokazal, katere fiziološke determinante je treba upoštevati v modelu, da dosežemo dobro skladnost med modelom in eksperimentalnimi rezultati, ki temeljijo na večcelični konfokalni mikroskopiji. Izkazalo se je, da lahko model dobro reproducira eksperimentalno opažene kompleksne dinamične vzorce, če so vključeni kombinacija heterogenih in stimulusno-odvisnih časovnih zamikov, variabilnost ravni ekscitabilnosti celic in heterogena sklopitev [1]. V nadaljevanju bomo model nadgradili z vključitvijo počasne oscilatorne komponente, ki jo upravlja paradigmatski Poincaréjev oscilator in odraža metabolno aktivnost beta celic. To nam omogoča preučevanje, kako kombinacija električne in metabolne sklopitve uravnava kolektivno ritmično aktivnost in kako se le-ta odraža na strukturi funkcionalnih mrež celic beta. Izgleda, da lahko električna sklopitev sama po sebi sinhronizira odzive, medtem ko vključitev metabolnih interakcij ne le dodatno izboljša sinhronost, temveč tudi razširi prostorski doseg interakcij, poveča število povezav znotraj funkcionalnih mrež in izboljša skladnost z eksperimentalnimi opažanji [2]. Na koncu bom izpostavil, da predlagani pristop fenomenološkega modeliranja, ki vključuje zelo malo parametrov, ni koristen le za pri-

dobivanje vpogledov v osnovne mehanizme oblikovanja večceličnih odzivov, ampak tudi opozarja na različne lastnosti, ki jih je treba upoštevati pri izgradnji celovitih in realističnih modelov omrežij celic beta.

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Deciphering the Intricacies of Beta Cell Network Dynamics: Lessons from Phenomenological Models

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Phenomenological models play a pivotal role in the study of complex biophysical systems. By providing a simplified yet accurate representation of real-world phenomena, they serve as a bridge between the intricate details of biophysical systems and our comprehension of their essential principles. This abstraction allows us to extract fundamental insights, reveal underlying mechanisms, and facilitate a deeper understanding of the system's dynamics. Moreover, it simplifies the interpretation of experimental data, making it easier to identify patterns and organizing principles. In this contribution I will present how phenomenological models can be used to decipher the intricacies of beta cell network dynamics. In these multicellular networks several hundred of beta cells work in synchrony to produce secretory pulses of insulin, a hormone crucial for controlling metabolic homeostasis. Their collective rhythmic activity is facilitated by intercellular coupling and affected by their multimodal activity due to networked feedback interactions of various oscillatory subsystems as well as by their functional heterogeneity. Consequently, the multicellular dynamics of beta cell populations is far from elemental and is characterized by intricate patterns of activity. Using a phenomenological model, I will first show which physiological determinants need to be considered in the model to achieve good agreement between the model and experimental results based on multicellular confocal microscopy. It turned out that the model can firmly reproduce the experimentally observed complex dynamical patterns if a combination of heterogeneous and stimulus-dependent time lags, variability in excitability levels and a heterogeneous coupling are incorporated [1]. Next, we upgrade the model by incorporating the slow oscillatory component, which is governed by the paradigmatic Poincaré oscillator and reflects the metabolic activity of beta cells. This eases us to investigate how the combination of electrical and metabolic coupling generates collective rhythmicity and shapes functional beta cell networks. It appears that, while electrical coupling alone can synchronize the responses, the inclusion of metabolic interactions not only further improves coordination but also expands the spatial range of interactions, increases the number of connections within the functional networks, and enhances the alignment with experimental observations [2]. I will conclude by emphasizing that the proposed phenomenological modelling approach that involves very few parameters is not only beneficial for getting

insights into basic mechanisms that shape the multicellular responses, but also points out the various attributes that should be considered by building up comprehensive and realistic models of beta cell networks.

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Perturbativni razvoj kvantnih spektrov in gravitacije okoli neskončnega števila dimenzij

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Perturbativna analiza spektrov linearnih operaterjev je dobro znana in neprecenljiva metoda za 'reševanje' Schrödingerjeve enačbe v kvantni mehaniki. Običajne analize razvijejo tak problem v obliki vrste v potencah sklopitvene konstante. V nekaterih primerih pa si je mogoče izmisliti tudi drugačen, nenavaden perturbativni parameter: $1/d$, kjer je d število prostorskih dimenzij. Tako v sistemih z gravitacijo kot tudi elektromagnetizmom je razvoj okoli $d = \infty$ možen zaradi dejstva, da elektromagnetne in gravitacijske sile padajo kot $1/r^d$ in se v $d = \infty$ efektivno lokalizirajo okoli vsakega točkastega naboja ali mase. Na tem predavanju bom predstavil zgodovino te metode in pokazal, kako jo lahko uporabimo za izpeljavo energijskih nivojev atomov vodika in celo helija. Nato pa bom razložil, kako deluje isti tip razvoja v gravitaciji in kako lahko uporabimo te rezultate s pomočjo holografske dualnosti za rekonstrukcijo nekaterih spektrov močno sklopljenih kvantnih teorij polja.

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Perturbative expansion of quantum spectra and gravity around an infinite number of dimensions

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Perturbative analysis of the spectra of linear operators is a well-known and invaluable method for 'solving' the quantum mechanical Schrödinger equation. Usually, this is done by expanding the problem as a power series in the coupling constant. In some cases, however, one may invent a different, unusual perturbative parameter 'from thin air': $1/d$, where d is the number of spatial dimensions. Both in systems with gravity and electromagnetism, such an expansion around $d = \infty$ is possible due to the fact that electromagnetic and gravitational forces scale as $1/r^d$ and in $d = \infty$ become effectively localised around each point charge or mass. In this talk, I will present the history of this method and show how one can use it to derive the energy levels of the Hydrogen and even the Helium atom. I will then explain how one can use the same expansion in gravity and utilise it with the help of the holographic duality to reconstruct certain spectra of strongly coupled quantum field theories.

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Stability and chaos of the duopoly model of Kopel: A study based on symbolic computations

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Since Kopel's duopoly model was proposed about three decades ago, there are almost no analytical results on the equilibria and their stability in the asymmetric case. The first objective of this talk is to analyze the asymmetric duopoly model of Kopel analytically by using several tools based on symbolic computations. We discuss the possibility of the existence of multiple positive equilibria and establish necessary and sufficient conditions for a given number of positive equilibria to exist. The possible positions of the equilibria in Kopel's model are also explored. Furthermore, if the duopolists adopt the best response reactions or homogeneous adaptive expectations, we establish rigorous conditions for the existence of distinct numbers of positive equilibria for the first time. The occurrence of chaos in Kopel's model seems to be supported by observations through numerical simulations, which, however, is challenging to prove rigorously. The second objective is to prove the existence of snapback repellers in Kopel's map, which implies the existence of chaos in the sense of Li-Yorke according to Marotto's theorem.

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Novi koncept detektorja za pozitronsko tomografijo (PET)

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V prispevku bom predstavil razvoj novih detektorjev žarkov gama, ki znatno izboljšajo časovno ločljivost zaznavanja in s tem omogočajo nov pristop pri načrtovanju naprav za slikanje s pozitronsko tomografijo, eno izmed najpomembnejših diagonostičnih metod. V tem novem konceptu je aparatura sestavljena iz posameznih detektorskih panelov, kar prinese veliko fleksibilnosti pri njeni uporabi. V prispevku bom predstavil razultate naših raziskav in načrte za njihovo nadaljevanje v okviru velikega evropskega EIC Pathfinder projekta PETVision.

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Novel detector concept for positron emission tomography (PET)

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In this contribution, I will present the development of new gamma-ray detectors that significantly improve the time resolution of detection and thereby enable a new approach in the design of positron-emission tomography imaging devices, one of the most important diagnostic methods. In this new concept, the apparatus consists of individual detector panels, which brings a lot of flexibility in its use. In the paper, I will present the results of our research and plans for their continuation within the framework of the large European EIC Pathfinder project PETVision.

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Precizijska fizika okusov pri Belle II

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Fizika okusov je ena od bistvenih Komponent Standardnega modela. Eksperimentalne šudije šbkih razpadov mezonov B in D pri eksperimentih Belle in BaBar so skupaj z odkritjem Higgsovega bozona na Velikem hadronskem trkalniku LHC omogocile koncno potrditev veljavnosti SM. Sedanja generacija precizijskih poskusov v fiziki okusov išče odstopanja od napovedi Standardnega modela. V prispevku bomo govorili o študijah anomalij v pri razpadih hadronov s kvarkom b in o študijah redkih razpadov, ki so zelo obetavna metoda za iskanje nove fizike.

Precision flavour physics with Belle II

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Flavour physics is one of the essential elements of the Standard Model. Experimental studies of weak decays of B and D mesons at B factories have, together with the discovery of the Higgs boson at LHC, provided the final confirmation of the validity of the SM. The present generation of precision flavour-physics experiments is looking for departures from the SM. We discuss studies of anomalies in b hadron decays, and studies of rare decays which are a very promising method for searching for new physics.

Advances in multimodal machine learning in healthcare

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Machine learning methods in healthcare have traditionally focused on using data from a single modality, limiting their ability to effectively replicate the clinical practice of integrating multiple sources of information for improved decision making. Here, we provide a review of recent advances in multimodal machine learning approaches in healthcare discussing different data fusion strategies and offering perspectives for the near future.

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Complexity: From Pattern Formation to Pattern Recognition

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According to several prominent authors, including Stephen Hawking, a main part of 21st century science will be on complexity research. The intuitive idea is that global patterns and structures emerge from locally interacting elements like atoms in laser beams, molecules in chemical reactions, proteins in cells, cells in organs, neurons in brains, transistors in electronic systems etc. (Mainzer 2007). Complex pattern formation has been reported from many disciplines (e.g., physics, chemistry, biology, brain research, engineering). The causes of complex pattern formation have been analyzed from various perspectives such as Schrödinger's (1948) order from disorder, Prigogine's (1980) dissipative structure, Haken's (1983) synergetics, Langton's (1990) edge of chaos etc. But concepts of complexity are often based on examples or metaphors only. We argue for a mathematically precise and rigorous definition of local activity as the cause of complex pattern formation which can be tested in natural as well as technical sciences by constructive methods. Recently, these results of complexity research have become important for machine learning of AI (artificial intelligence) systems (e.g., neural networks, cognitive AI-systems, robots). Instead of complex pattern formation in nature, complex pattern recognition of artificial neural networks (ANN) is considered which is modeled in statistical learning theory. But, ANN-systems are only simulated on digital computers with von-Neumann architectures which run into severe problems of energy consumption (von-Neumann bottleneck) in the future - in contrast to the highly energetically efficient biological brains. Therefore, neuromorphic systems with more brain-oriented computing should be considered also for hardware realization. The research target is sustainable computing and AI with respect to energy and environment.

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Matematično modeliranje izločanja insulina in glukagona

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Trebušna slinavka je pomemben organ, ki med drugim skrbi za izločanje insulina in glukagona kot dveh ključnih hormonov za uravnavanje glukoze in drugih metabolitov v našem telesu. Z metodo matematičnega modeliranja proučujemo procese v celicah alfa in beta trebušne slinavke in napovedujemo izločanje glukagona in insulina pri različnih pogojih. Pomembne so napovedi, ki kažejo na bolezenska stanja, ko so procesi deregulirani. Še posebej se osredotočamo na vlogo mitohondrijev kot ključnih celičnih organelov za produkcijo celične energije v obliki ATP in zagotavljanja anaplerotičnih metabolnih poti. Z modelnimi napovedmi uspešno napovemo patologije, ki so povezane z deregulacijo mitohondrijske funkcije.

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Mathematical modeling of insulin and glucagon secretion

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The pancreas is an important organ that, among other functions, is responsible for the secretion of insulin and glucagon, two key hormones for regulating glucose and other metabolites in our body. Through the method of mathematical modeling, we study the processes in the alpha and beta cells of the pancreas and predict the secretion of glucagon and insulin under various conditions. Predictions indicating disease states, where processes are deregulated, are important. We particularly focus on the role of mitochondria as key cellular organelles for the production of cellular energy in the form of ATP and anaplerotic metabolic pathways. With model predictions, we successfully forecast pathologies associated with the deregulation of mitochondrial function.

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Simulacija holesterika v vijačno simetrični ograditvi

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Predstavil bom rezultate numeričnega modeliranja dvojne vijačne strukture holesteričnega tekočega kristala v vijačno simetrični ograditvi. Simulacija pojasni novo holesterno strukturo, ki je bila nedavno eksperimentalno opažena. Vijačna simetrija tri-dimenzionalni problem simulacije omeji na dve dimenziji, kar znatno poenostavi numerično reševanje. Tekoči kristal opišemo z Landau-de Gennesovim modelom v eno-konstantni aproksimaciji. Za različne oblike in različne vrednosti zvitja tekoče kristalne strukture analiziramo dobljena metastabilna stanja. Pri vrednostih parametrov, ki se ujemajo z eksperimentalnimi podatki, uspemo simulirati metastabilno stanje, ki ima dvojni zvoj z istima ročnostima in lokalizirana defektna območja v konicah vboklin v vijačni strukturi. V treh dimenzijah dobimo torej dve linijski zviti disklinaciji, s čimer potrdimo razumevanje nastale strukture.

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Simulation of a cholesteric in a helical confinement

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Recently, a novel cholesteric structure has been experimentally observed. I will discuss the numerical modelling of this doubly helical structure in a helical confinement. Helical symmetry reduces the simulation problem to two dimensions, thus making the simulation much faster. Cholesteric is modeled within the Landau-de Gennes formalism using one-constant approximation. We simulate different possible helical shapes and differently twisted structures and analyze the resulting meta-stable states. For the shape and parameter values that correspond to the experimental data we succeed in obtaining a meta-stable state with a double twist director structure with the same sign and two localized defects in the two cusps of the twisted structure. In three dimensions that corresponds to two twist disclinations.

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Integrable open quantum systems

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In physics, most problems are typically solved using approximations. However, there exist some rare cases where the large amount of symmetries makes them exactly solvable. Those systems are called Integrable.
In this talk, I will introduce the boost automorphism mechanism: a systematic approach for constructing new integrable spin chains characterized by a R-matrix, solution of the Yang-Baxter equation. The method consists in starting with an ansatz for the Hamiltonian and then restricting it to belong to an integrable model. This method has applications in different areas of physics, from condensed matter to high-energy physics. I will explain how we used it to provide the first systematic classification of integrable Lindbladians: open quantum system where the environmental response is Markovian. I will present one of the new models we discovered and discuss its properties: it corresponds to the first integrable next-to-nearest neighbour deformation of the Hubbard model.

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Quantum Chromodynamics: 50 Years After Its Invention

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In the early 1960's strongly interacting elementary particles were classified along the symmetry group $SU(3)$. It was suggested that hadrons behave as if they were constituted by substructures, then named as quarks [1] or aces [2]. It was left open, if these subunits merely reflect symmetries or should be understood as particles.

By 1968, a SLAC-MIT study of deep-inelastic electron scattering produced first experimental evidence that the proton contains point-like constituents [3]. These findings [4,5] were awarded the Nobel prize only much later (in 1990). 'Partons' got identified with quarks, but it took some time to develop the theory of their interactions. In late 1972, Fritzsch and Gell-Mann proposed a gauge theory of $SU(3)_C$ [6]. It's generators, the gluons, mediated the strong interactions. From then on the pertinent color gauge theory, quantum chromodynamics (QCD), has generally been assumed as the fundamental theory of the strong/hadronic force [7].

Now, 50 years later, QCD is not yet solved completely. The corresponding millenium prize is still to be earned [8] ! However, many methods have been developed to gain reliable results, such as perturbation theory, effective field theories, quark models etc. I will review several of these approaches and discuss corresponding results, manifesting our present understanding of hadronic physics.

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Kvantni mnogodelčni kaos

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Kvanti kaos (v pretežno enodelčnih sistemih) je bil zelo živahno raziskovalno področje v 1980ih in 1990ih. V zadnjih letih pa se je področje kvantnega kaosa spet zelo oživilo okrog kvantnega mnogodelčnega problema, kar je pritegnilo teoretične fizike iz zelo raznoterih skupnosti, od fizike kondenzirane materije, kvantne optike in kvantne informatike, pa do kvantne gravitacije. Ena od najbolj splošnih in robustnih lastnosti kvantno-kaotičnih sistemov je aplikativnost teorije slučajnih matrik.

Po motivacijskem uvodu v področje kvantnega kaosa se bom posvetil predvsen fascinantnemu problemu presenetljive učinkovitosti teorije slučajnih matrik za popis spektralnih fluktuacij v razsežnih kvantnih sistemih na mrežah. Pred kratkim smo identificirali razred takšnih sistemov z lokalno interakcijo, kjer lahko matematično rigorozno pokažemo ujemanje statističnih fluktuacij lastnih (kvazi)energij, karakterizirano s t.i. spektralnim oblikovnim faktorjem, ter teorijo slučajnih matrik. Takšni *dvojno unitarni sistemi* vsebujejo celotno ergodično hierarhijo dinamičnih režimov, od integrabilnosti, ne-ergodičnosti, do ergodičnosti, mešanja in maksimalnega (kvantnega) kaosa. Dvojno unitarni sistemi omogočajo analitičen izračun prostorsko-časovnih korelacijskih funkcij lokalnih opazljivk in so zelo primerni za eksperimentalni študij v aktualnih kvantnih simulatorjih.

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Quantum Many-Body Chaos

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Quantum chaos (of mostly single particle problems) has been a fruitful interdisciplinary arena of research in 1980s' and 1990s'. In recent years, the field has dramatically revived around the quantum many-body problem gathering very diverse communities of theoretical physicists ranging from condensed matter, quantum optics and quantum information, to quantum gravity. One of the most general characteristics of quantum chaotic systems is the ubiquitous applicability of random matrix theory.

After a general introduction to the field, I will focus specifically on the fascinating problem of 'unreasonable effectiveness' of random matrix theory for description of spectral fluctuations in extended quantum lattice systems. A class of locally interacting spin systems has been recently identified where the fundamental measure of (quasi)energy level fluctuations, the spectral form factor, is proven to match with random matrix theory, and where spatiotemporal correlation functions of local observables as well as some measures of dynamical complexity can be calculated analytically. These, so-called dual unitary systems, include the whole 'ergodic hierarchy' of dynamics: integrable, non-ergodic, ergodic, and generically, (maximally) chaotic cases, and are ideally suited for experimental studies on the current generation of quantum simulators.

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Kvantni kaos v mešanih sistemih: Potenčno pojemanje deleža mešanih stanj v semiklasični limiti

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Kvantni kaos je študij lastnosti lastnih stanj, energijskih spektrov, dinamike, Wignerjevih in Husimijevih funkcij (v kvantnem faznem prostoru) sistemov, katerih klasični analogon je kaotičen, ali delno kaotičen [3]. Generični, tipični sistemi, delno kaotični, imajo v faznem prostoru v sobivanju regularna in kaotična območja. Takšna struktura klasičnega faznega prostora se zrcali v lastnostih Wignerjevih in Husimijevih funkcij v kvantnem faznem prostoru, kjer opazimo regularna stanja na invariantnih torusih, kaotična stanja v kaotičnih območjih (kjer so lahko lokalizirana), ter mešana stanja, ki so povezana z različnimi mehanizmi sklopitve regularnih in kaotičnih območij. Princip enakomerne semiklasične kondenzacije Wignerjevih in Husimijevih funkcij (Robnik 1998, [2]) napoveduje v striktni semiklasični limiti dovolj majhne efektivne Planckove konstante obstoj zgolj regularnih stanj na invariantnih torusih ter kaotičnih stanj v klasično kaotičnih območjih, medtem ko se delež mešanih stanj v semiklasični limiti zmanjšuje, kar je v skladu z Berry-Robnikovo sliko [1]. Predstavil bom stacionarni vidik ter opis kvantnih lastnih stanj v kvantnem faznem prostoru, ter pokazal prvo kvantitativno fenomenološko evidenco za potenčno pojemanje deleža mešanih stanj za primer t.i. limonastih biljardnih sistemov [4]. Ti rezultati so potrjeni tudi v drugih sistemih, kot so brcana vrtavka [5], Dickov model [6] ter Fermi-Pasta-Ulam-Tsingou sistem [7], kar kaže na univerzalnost potenčne zakonitosti, vendar z eksponenti, ki so specifični za sistem, in niso univerzalni.

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Quantum chaos in mixed-type systems: Power-law decay of the fraction of mixed eigenstates in the semiclassical limit

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Quantum chaos is a study of properties of eigenstates, energy spectra, dynamics, Wigner and Husimi functions (in the quantum phase space) of systems, whose classical analogon is chaotic, or partially chaotic [3]. Generic, typical systems, partially chaotic, have in the phase space coexisting regular and chaotic regions. Such structure of the classical phase space is reflected in the properties of the Wigner and Husimi functions in the quantum phase space, where we observe regular states on the invariant tori, chaotic states in chaotic regions (which can be localized), and mixed states which are connected with various mechanisms of coupling between the regular and chaotic regions. The Principle of uniform semiclassical condenstation (PUSC) of Wigner and Husimi functions (Robnik 1998, [2]) predicts in the strict semiclassical limit of sufficiently small effective Planck constant, the existence of merely regular states on invariant tori, and chaotic states on the classically chaotic regions, while the relative fraction of the mixed states decays, in agreement with the Berry-Robnik picture [1]. I shall present the stationary aspect and description of quantum eigenstates in the quantum phase space, and show the first quantitative phenomenological evidence for the power-law decay of the relative fraction of the mixed states in the case of so-called lemon billiards [4]. These results are confirmed also in other systems like kicked top [5], Dicke model [6] and the Fermi-Pasta-Ulam-Tsingou system [7], which indicates the universality of the power law, but with exponents which are system dependent, and thus not universal.

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Invariante in reverzibilnost v polinomskih sistemih NDE

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Najprej proučujemo povezavo med invariantami nekaterih delovanj grup in časovno reverzibilnostjo v razredu dvorazsežnih polinomskih sistemov z 1:-1 resonantno singularnostjo v izhodišču. Časovna reverzibilnost je tesno povezana z mnogoterostjo Sibirskega, ki je vsebovana v centralni mnogoterosti, in vemo, da vsak časovno reverzibilen sistem premore lokalni analitični prvi integral v okolici izhodišča. Podamo nov algoritem za izračun množice generatorjev ideala Sibirskega in nekatere algebraične lastnosti tega ideala.

V preostanku raziskujemo posplošitev pojma časovne reverzibilnosti v tri razsežnih sistemih z $1 : \zeta : \zeta^2$ resonančno singularnostjo v izhodišču (kjer je ζ primitivni tretji koren enote). Preučujemo povezavo te reverzibilnosti z invariantami določenih delovanj grup v prostoru parametrov sistema in z Lawrence-ovimi ideali.

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Invariants and reversibility in polynomial systems of ODEs

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We first investigate the interconnection of invariants of certain group actions and time-reversibility of a class of two-dimensional polynomial systems with 1:-1 resonant singularity at the origin. The time-reversibility is related to the Sibirsky subvariety of the center (integrability) variety and it is known that every time-reversible system has a local analytic first integral at the origin. We propose a new algorithm to obtain a generating set for the Sibirsky ideal of such polynomial systems and investigate some algebraic properties of this ideal.

Then, we discuss a generalization of the concept of time-reversibility in the three dimensional case considering the systems with $1:\zeta:\zeta^2$ resonant singularity at the origin (where ζ is a primitive cubic root of unity) and study a connection of such reversibility with the invariants of some group actions in the space of parameters of the system and Lawrence ideals.

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Brezmrežne simulacije večfizikalnih in večnivojskih problemov s strjevanjem

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V prispevku najprej predstavimo koncept povezanih simulacij strjevanja večsestavinskih sistemov na več merilih ob prisotnosti zunanjih polj. Pri tem so makroskopski modeli formulirani na podlagi teorije idealne mešanice, mezoskopski na podlagi celičnih avtomatov in mikroskopski na podlagi faznega polja. V modelih upoštevamo prenos mase, energije, gibalne količine in sestavin. Fazni diagram je vključen na podlagi vzvodnega pravila, kašasto področje pa s porozno plastjo. Predstavimo inovativne brezmrežne rešitve na vseh treh nivojih, ki temeljijo na konceptu močne formulacije, razdelitve področja na poddomene in uporabo različnih avtomatskih prilagoditvenih strategij. Na koncu predstavimo uporabo nekaterih razvitih modelov pri snovanju vodilnih tehnologij.

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Meshless simulation of multiphysics and multiscale solidification problems

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In this paper, we first present the concept of coupled simulations of solidification of multicomponent systems at multiple scales in the presence of external fields. The macroscopic models are formulated on the basis of the ideal mixture theory, mesoscopic models on the basis of cellular automata and microscopic models on the basis of the phase field. The models take into account the transfer of mass, energy, momentum and species. The phase diagram is included based on the lever rule, and the mushy zone with the porous layer. We present innovative meshless solutions at all three levels based on the concept of strong formulation, partitioning the domain into subdomains, and use of different automatic adaptation strategies. Finally, we present the use of some developed models in the creation of leading technologies.

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Nonequilibrium quantum dynamics in trapped ultracold mixtures: From quenching across phase boundaries to impurity transport

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Our focus is the correlated non-equilibrium quantum dynamics for a binary mixture of ultracold trapped atoms. Three different scenarios will be addressed. First we explore the quench dynamics of a binary Bose–Einstein condensate crossing the miscibility–immiscibility threshold. Increasing the interspecies repulsion leads to the filamentation of the density of each species, involving shorter wavenumbers and longer spatial scales in the many-body approach compared to mean-field theory. These filaments appear to be strongly correlated and exhibit domain-wall structures. We simulate single-shot images to connect our findings to possible experimental realizations.

Next we explore the dynamical transport of an impurity between different embedding majority species which are spatially separated in a double well. The transfer and storage of the impurity is triggered by dynamically changing the interaction strengths between the impurity and the two majority species. We find a simple but efficient protocol consisting of linear ramps of majority-impurity interactions at designated times to pin or unpin the impurity. We analyze the dynamics in terms of single-particle densities, entanglement growth and provide an effective potential description involving mean-fields of the interacting components.

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Numerical methods of chaos detection

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Determining the chaotic or regular nature of orbits of dynamical systems is a fundamental problem of nonlinear dynamics, having applications to various scientific fields. The most commonly employed method for distinguishing between regular and chaotic behavior is the evaluation of the maximum Lyapunov exponent (MLE) σ_1, because if $\sigma_1 > 0$ the orbit is chaotic [1 and references therein]. The main problem of using this chaos indicator is that its numerical evaluation may take a long -and not known a priori- amount of time to provide a reliable estimation of the MLE's actual value. Over the years, many techniques have been developed, which try to overcome this problem (review presentations of some of them can be found in [2]).

In this talk we will focus our attention on two very efficient methods of chaos detection: the Smaller (SALI) and the Generalized (GALI) Alignment Index techniques [3-9]. We will first recall the definitions of the SALI and the GALI and will briefly discuss the behavior of these indices for conservative Hamiltonian systems and area-preserving symplectic maps, emphasizing that these methods are based on the evolution of more than one deviation vectors from the studied orbit, in contrast to the computation of the MLE where only one deviation vector is needed. Then, we will explain how one can use these methods to investigate the dynamics of time-dependent dynamical systems by considering a barred galaxy model whose parameters evolve in time [10].

We will also present some recently introduced methods to estimate the chaoticity of orbits in conservative dynamical systems from computations of Lagrangian descriptors (LDs) [11, 12] on short time scales. In particular, we will consider methods based on the difference and the ratio of the LDs of neighboring orbits, as well as a quantity related to the finite-difference second spatial derivative of the LDs [13, 14]. These indicators can correctly identify the chaotic or regular nature of orbits to better than 90% agreement with results obtained by the SALI method. These findings indicate the capability of LDs to efficiently identify chaos in conservative dynamical systems without knowing the variational equations (tangent map) of continuous (discrete) time systems needed by traditional chaos indicators.

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Spin resonance without a spin: A microwave analog

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Following a suggestion of Joyner et al. [1] we previously realized a microwave network with a particular symmetry simulating a spin 1/2 [2,3]. In this work the analogy is promoted even further towards a microwave analog of a magnetic resonance experiment. The network consists of two identical subgraphs coupled by a pair of bonds with a length difference corresponding to a phase difference of π for the waves traveling through the two bonds. As a consequence all eigenvalues appear as Kramers doublets. Detuning the length difference from the π condition Kramers degeneracy is lifted, which may be interpreted as a Zeeman splitting of a spin 1/2 in a magnetic field. The lengths of another pair of bonds are modulated periodically with frequencies of some 10 MHz by means of diodes, thus emulating a magnetic radiofrequency field. Features well-known from nuclear magnetic resonance such as the transition from the laboratory to the rotating frame, or Lorentzian shaped resonance curves can thus be realized.

This is a joint work together with Tobias Hofmann, Finn Schmidt, Philipps University of Marburg, and Ulrich Kuhl, Université Côte d'Azur of Nice.

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Fazni prehodi z zlomom ergodičnosti

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Kvantna termalizacija in ergodičnost sta lastnosti, ki veljata za večino fizikalnih sistemov. Kljub temu pa se nekateri sistemi ne podrejajo tem zakonitostim in kažejo drugačne lastnosti. To vodi do prehoda med dvema različnima fazama: tisto, v kateri sistem termalizira, in tisto, v kateri ne termalizira. Prehod lahko opazimo v različnih lastnostih sistema, denimo v lastnostih lastnih stanj in spektra, naravi transporta naboja in energije, in tako dalje. V termodinamski limiti te prehode imenujemo fazni prehodi z zlomom ergodičnosti.

V seminarju se bomo osredotočali na to, kako zaznati fazni prehod z zlomom ergodičnosti skozi vidik neravnovesne kvantne dinamike. Eden od načinov študije dinamike je osredotočanje na skalirno invarianco, ker pomeni, da sistem ne spremeni svojega obnašanja ob spremembi časovne ali prostorske skale. Skalirna invarianca je v ergodičnih sistemih uveljavljen pojav ob dolgih časih, kot je denimo pojav t.i. prečke (ang. *ramp*) v spektralnem oblikovnem faktorju. Pokazali bomo, da se skalirna invarianca v sistemih na prehodu med ergodično in neergodično fazo pojavi že ob precej krajših časih. Osredotočali se bomo na dinamiko dveh količin, t.i. preživetvene verjetnosti začetnega stanja (ang. *survival probability*) in spektralnega oblikovnega faktorja, ter obravnavali tako kvadratne modele kot modele z interakcijo.

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Ergodicity breaking phase transitions

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Quantum thermalization and ergodicity are principles that most physical systems obey. However, some systems may deviate from these principles and show a different behavior. This can cause a transition between two contrasting phases: one where the system thermalizes and one where it does not. The transition can be observed in various aspects of the system, such as the properties of its eigenstates and spectra, the nature of charge and energy transport, and so on. In the thermodynamic limit, these transitions are known as ergodicity breaking phase transitions.

I will talk about how to detect the ergodicity braking phase transitions based on their nonequilibrium dynamics. One way to study the dynamics is to look at the scale invariance, which means that the system does not change its behavior when the scale of time or space is changed. Scale invariance is common at long times in ergodic systems as shown, e.g., by the ramp feature in the spectral form factor. However, we find that scale invariance also appears at shorter times in systems that are at the transition point between the ergodic and nonergodic phases. We investigate the scale invariant dynamics of two quantities: the survival probability and the spectral form factor, and we study both quadratic and interacting systems.

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Kvantni in kvantno-navdihnjeni algoritmi za analitiko grafov

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Grafne nevronske mreže so zmogljivo orodje za analitiko grafov s strojnim učenjem. Njihova široka uporabnost pri analizi bioloških in družbenih sistemov, kemijskih formul, pa tudi besedil in slik, je v znanstveni skupnosti vzbudila veliko zanimanje za razvoj hitrejših, natančnejših in učinkovitejših algoritmov. Ključna pomanjkljivost sedanjih algoritmov je, da so zaradi prepletanja interakcij dolgega in kratkega dosega zahtevni za procesiranje na trenutnih CPU/GPU in posledično računsko kompleksni. Nedavni pristop k temu problemu je uporaba kvantnega računalništva, ki naslavlja prepletanje med interakcijami dolgega in kratkega dosega s pomočjo kvantne prepletenosti. Po predstavitvi osnov strojnega učenja na kvantnih računalnikih bom predstavil nekatere nedavne rezultate na tem področju in zaključil s predstavitvijo študije primera uporabe kvantnih grafnih nevronskih mrež za segmentacijo.

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Recent developments in developing quantum and quantum-inspired algorithms for graph analytics

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Graph neural networks are a powerful tool for analysis of graphs with machine learning. Their widespread usefulness in analysis of biological and social systems, chemical compositions, as well as text and images, has sprouted large interest from scientific community in developing faster, more accurate and more efficient algorithms. The key downside of current algorithms is that they are notoriously computationally difficult, due to the interplay between long-range and short-range interactions, which makes the processing ill-suited for current CPUs/GPUs. A recent approach to the problem is the use of quantum computing to address the interplay between long and short-range interactions through quantum entanglement. After introducing the basics of machine learning on quantum computers, I will discuss some recent results in the field and finish with a presentation of a case study of a quantum graph neural network applied to classification.

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Emergence of unitary symmetry of microcanonically truncated operators in chaotic quantum systems

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We study statistical properties of matrix elements entering the eigenstate thermalization hypothesis by studying the observables written in the energy eigenbasis and truncated to small microcanonical windows. We put forward a picture, that below certain energy scale collective statistical properties of matrix elements exhibit emergent unitary symmetry. In particular, below this scale the spectrum of the microcanonically truncated operator exhibits universal behavior for which we introduce readily testable criteria. We support this picture by numerical simulations and demonstrate existence of emergent unitary symmetry scale for all considered operators in chaotic many-body quantum systems. We discuss operator and system-size dependence of this energy scale and put our findings into context of previous works exploring emergence of random-matrix behavior in narrow energy windows.

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Power-law decay of the fraction of the mixed eigenstates in different quantum systems

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The properties of the mixed eigenstates in a generic quantum system with a classical counterpart that has mixed-type phase space, although important to understand various fundamental questions that arise in both theortical and experimental studies, are still less known. Here, we perform an analysis of the features of mixed eigenstates in two different quantum systems, namely kicked-top model and Dicke model. By using the phase-space overlap index, we show that the mixed eigenstates appear due to various tunneling processes between different phase-space structures, while the regular and chaotic eigenstates are, respectively, associated with invariant tori and chaotic components in phase space. We investigate how the probability distribution of the phase-space overlap index evolves with increasing system size. In particular, we demonstrate that the relative fraction of the mixed eigenstates shows a power-law decay as the system size increases, indicating that only purely regular and chaotic eigenstates are left in the strict semiclassical limit. Our results provide further verification of the principle of uniform semiclassical condensation of Husimi function and confirm the correctness of the Berry-Robnik picture.

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Every raindrop has an exceptional history

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Rainfall from ice-free clouds requires collisions of very large numbers of microscopic droplets to create every raindrop, and the collision rate for the first few droplet coalescences is very low, typically less than one per hour [1]. The onset of rain showers can be surprisingly rapid, much faster than the mean time required for a single collision. One possible explanation [2,3] is that every raindrop is the result of a sequence of exceptionally rare events, where the first few collisions happen unusually quickly. The talk will discuss how large-deviation theory [4] can give a quantitative justification of this suggestion. The calculation [5] shows that a rain shower can occur on a timescale which is *less* than the mean time for the first of the approximately one million collisions which must occur to make each raindrop. Recent results [6] on the growth history of those 'lucky' droplets will be presented. I shall also comment on the whether the calculations are relevant to planet formation, which is usually regarded as another example of a runaway aggregation process.

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Spacing ratios of mixed-type systems

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The distribution of the consecutive level-spacing ratio is now widely used as a tool to distinguish regular from chaotic quantum spectra, mostly due to its avoiding of the numerical spectral unfolding. Similar to the use of the Rosenzweig-Porter approach to obtain the Berry-Robnik distribution of level-spacings in mixed-type systems [1], in this work we extend this approach [2] to derive analytically the distribution of spacing ratios [3], for random matrices comprised of independent Poisson blocks and GOE blocks. One application of this distribution is that one can use it to characterize the relative size of the integrable part of phase space, which we have verified numerically in quantum maps such as quantum kicked rotor and quantum kicked top, and in continuous system such as quantum three-particle FPUT [4].

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Ko se površnost izplača: nehermitskost in anomalna relaksacija

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V kvantni mehaniki smo običajno vajeni delati z unitarno evolucijo in pripadajočimi hermitskimi generatorji. A kadar nas zanima le del opazljivk, to naravno privede do nehermitskosti. Na konkretnem primeru Markovskega procesa bom pokazal, kako lahko dinamika v takem primeru, v nasprotju z običajno folkloro, ki pravi, da je relaksacijski čas dan s končno spektralno režo, privede to fantomske relaksacije, ki ni določena z nobeno lastno vrednostjo. To nas bo pripeljalo do koncepta psevdospektra in spoznanja, da se pri delu z nehermitskimi operatorji lahko zgodi, da je eksakten rezultat napačen, mičkeno napačen pa pravilen.

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When being sloppy helps: Non-Hermiticity and anomalous relaxation

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Quantum mechanics is ruled by Hermitian generators inducing unitary propagation, nevertheless, when tracing out some degrees of freedom one can end up with non-Hermitian operators. An example is entanglement or out-of-time-ordered correlation functions in random circuits, where the relaxation dynamics is described by a non-Hermitian Markovian matrix with a finite gap. Naturally one would expect that the relaxation, i.e., the rate of generating entanglement, will be given by this finite spectral gap. However, this is not the case. Rather, in the thermodynamic limit the rate is given by a phantom eigenvalue – an "eigenvalue" that is not in the spectrum. Resolution of this puzzle will lead to a pseudospectrum and a realization that when dealing with non-Hermitian matrices being exact can actually be wrong, while being slightly wrong is correct.

References

[1] M. Žnidarič, *Solvable non-Hermitian skin effect in many-body unitary dynamics*, arXiv:2205.01321 (2022).

[2] L. N. Trefethen and M. Embree, *Spectra and Pseudospectra* (Princeton, 2005).

Informiranje javnosti o (astro)fizikalnih raziskovalnih rezultatih

TOMAŽ ZWITTER

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Informiranje javnosti je dolžnost, za katero bi morala poskrbeti vsaka raziskovalna skupina, ki je javno financirana. Ob tem koristi tudi pri pridobivanju novih kadrov. Ko se lotimo take naloge, si je dobro zamisliti, kaj želimo sporočiti, pri tem pa upoštevati, komu govorimo. V predstavitvi se bom osredotočil na nekaj praktičnih navodil, kaj delati in česa ne, kaj so pasti in kaj prednosti. Končen zaključek bo, da tak angažma zahteva precej razmisleka in posledično tudi časa. Povedano bom ilustriral z nedavnimi raziskovalnimi rezultati in praktičnini primeri, ki segajo od motivacije osnovnošolskih otrok do nastopov v elektronskih medijih in pisanja učbenika za študente.

Public outreach on research results in (astro)physics

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Public outreach can be considered a duty which is to be honored by any publicly financed research group. Besides, it brings visibility which may have its benefits in attracting good students. When planning for such a task it is important to define the message we want to convey and to take into account the type of target audience. I shall focus on some practical advice on what to do and what to avoid, what can be problematic and what is not. An obvious conclusion will be that this type of activity demands good planning and therefore quite a bit of time. I will use examples of recent research results which have been presented to different audiences, from talks to school children to presentations for general public in electronic media and to writing of a textbook for students.

Program Koncerta v hotelu HABAKUK
četrtek, 14. 12. 2023, ob 19.00

Izvajalec: Nikolaj Sajko (violončelo), Maja Gombač (klavir)
Performing: : Nikolaj Sajko (cello) Maja Gombač (piano)

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Gabriel Faure: Elegija op. 24

Robert Schumann: Fantazijske skladbe, op. 73 / Fantasy Pieces Op. 73
Zart und mit Ausdruck
Lebhaft, leicht
Rasch und mit Feuer

Peter Iljič Čajkovski: Sentimentalni valček / Sentimental waltz

Felix Mendelssohn: Pesem brez besed, op. 109 / Song without words, Op. 109

Camille Saint-Saëns: Labod / The Swan

Alexander Scriabin: Romanca / Romance

Astor Piazzolla: Oblivion

Ludwig van Beethoven: 3. stavek iz Sonate št. 3 v A-duru, op. 69 za klavir in violončelo / 3rd movement from Sonata no. 3 in A major, Op. 69 for piano and cello

Edward Elgar: Salut d'Amour

Nikolaj Sajko je diplomiral iz violončela v razredu Cirila Škerjanca na Akademiji za glasbo v Ljubljani, kjer je končal tudi znanstveni magistrski študij, podiplomsko pa se je v solistični igri izpopolnjeval na Univerzi Antona Brucknerja v Linzu. Je dobitnik Klasinčeve diplome in nagrade Antonia Tarsie, pomembne uvrstitve pa je dosegel tudi na državnih in mednarodnih tekmovanjih mladih glasbenikov v Gorici, Lieznu, Zagrebu in Ljubljani. Bil je član mednarodnega mladinskega orkestra Gustav Mahler in član Svetovnega orkestra glasbene mladine. Od leta 2006 je namestnik soločelista v Simfoničnem orkestru SNG Maribor ter poučuje na Konservatoriju za glasbo in balet v Mariboru. Od leta 2012 programsko vodi cikel komornih koncertov Carpe artem.

Maja Gombač je študij klavirja z odliko zaključila na Akademiji za glasbo v Ljubljani pri prof. Hinku Haasu, leta 2018 pa še na Univerzi za upodabljajočo umetnost v Grazu pri prof. Markusu Schirmerju, kjer je prejela najvišjo oceno s pohvalo. Tekom študija se je v okviru mednarodne izmenjave eno leto izpopolnjevala tudi pri prof. Imreju Rohmannu na Mozarteumu v Salzburgu. Kot solistka je prvič nastopila s komornim orkestrom Slovenske filharmonije ter z njimi izvedla Bachov koncert v f - molu. Sledile so izvedbe mnogih drugih klavirskih koncertov: Griegov koncert (Simfoničniorkester RTV Slovenija, orkester SNG Opera in balet Maribor, Jenska filharmonija), Beethovnov koncert št. 5 (Orkester SNG Opere in baleta Ljubljana), Mozartovi koncerti št. 2, 3, 4, 21 in 23 (Luksemburški komorni orkester) in Beethovnov trojni koncert (Ruski filharmonični komorni orkester). Kot del zasedbe je pet let sodelovala tudi s Salzburško filharmonijo. Je nagrajenka številnih mednarodnih tekmovanj (Paul Harris, Davorin Jenko, Antonio Salieri, Rotary Club Valencia, Karlovac, Martha Debelli) in državnega tekmovanja TEMSIG, kjer je prejela dve zlati odličji kot solistka in kot komorna glasbenica. Za svoje umetniške dosežke je prejela Prešernovo nagrado Akademije za glasbo v Ljubljani. Od marca 2020 je redno zaposlena na Univerzi za glasbo in upodabljajočou metnost v Gradcu, kjer poučuje klavir.

Nikolaj Sajko graduated in cello performance at the Academy of Music in Ljubljana, where he also completed his Master's degree, and postgraduate studies in solo performance at the Anton Bruckner University in Linz. He has won the Klasinc Diploma and the Antonio Tarsia Prize, and has also achieved important rankings at national and international competitions for young musicians in Gorizia, Liezen, Zagreb and Ljubljana. He was a member of the Gustav Mahler International Youth Orchestra and a member of the World Youth Orchestra. Since 2006 he has been the assistant principal cello of the Symphony Orchestra of Slovene National Theatre in Maribor and teaches at the Maribor Conservatory of Music and Ballet. Since 2012 he has been the programme director of the chamber concert series Carpe artem.

Based in Austria, **Maja Gombač** belongs to the new generation of Slovenian classical pianists. She is an accomplished piano pedagogue currently teaching at at the University of Music and Performing Arts in Graz. Maja has already appeared in a wide range of concert venues, including international festivals in Austria, Germany, Italy, Switzerland, France, Luxembourg, United Kingdom and Croatia, where she performed as a soloist or in various chamber ensembles. In addition to her concert activity, she frequently recorded for the Slovenian National Radio and Television. She debuted as a soloist with the Slovenian Philharmonic Chamber Orchestra, performing the Concerto No. 5 in F minor by J. S. Bach. Later on, she gave performances of many other Piano Concertos; Edward Grieg Concerto op. 16 (RTV Slovenia Symphony Orchestra, Slovenian National Opera Orchestra), L. Van Beethoven Concerto No. 5 (Slovenian National Opera Orchestra), Mozart Concertos No. 2, 3, 4, 21 and 23 (Luxembourg Chamber Orchestra), Beethoven Triple Concerto (Russian Philharmonic Chamber Orchestra KLASSIKA). Maja is a multiple prize-winner at international music competitions and an awardee of two Gold Medals at the Slovenian national competition TEMSIG, along with numerous Special Prizes. She was a recipient of scholarships awarded by Slovenian Ministry of Culture, Slovenian State Merit Foundation, Rotary Club, Martha Debelli Foundation, Josef Dichler Foundation and University of Music and Performing Arts Graz. Furthermore, she received the "Preseren Prize" for her outstanding academic achievements. Maja started to study piano performance at the Ljubljana Academy of Music with professor Hinko Haas and continued at the University of Music and Performing Arts Graz with professor Markus Schirmer, where she finished her Master's Degree in 2018 with distinction. She also attended numerous masterclasses, including some held by Robert Levin, Imre Rohmann, Klaus Helwig, Cyprien Katsaris, Igor Latzko, Vladimir Viardo and Konstantin Bogino.

Program Koncerta v hotelu HABAKUK
petek, 15. 12. 2023, ob 19.00

Izvajalec: Godalni kvartet Al Fine / Performing: String Quartet Al Fine

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B. Ipavec: Serenada za godala / B. Ipavec: The Serenade for the Strings

I. Allegro moderato

II. Menuetto

III. Andante con variazioni

IV. Finale

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P. I. Čajkovski: Plesi iz suite Hrestač (priredba za godalni kvartet) /

P. I. Tschaikowsky: Dances from The Nutcracker Suite (arranged for String Quartet)

Ples sladkorne vile / Dance of the Sugar Plum Fairy

Ples piščali / Dance of the Mirlitons

Cvetlični valček / Waltz of the Flowers

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C. Debussy: Deklica z lanenimi lasmi / The Girl with the Flaxen Hair

G. Bregović (arr. P. Kranjec): Ausencia

E. Elgar: Salut d'Amour

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F. Kreisler: Small Viennese March

L. Anderson: Plink - Plank - Plunk

P. Beltran/P. Prado: Sway, Cherry Pink

J. Marks (arr. B. Ligon): Rocking Around the Christmas Tree

Godalni kvartet Al Fine

Nocojšnji koncert je posvečen duhu prazničnega časa, ki je pred nami. Časa, ki je prežet s kančkom tradicionalnosti ter obogaten s čarobnostjo pričakovanja. Obdobje notranjega veselja, spominov in upanja, pa tudi duhovitosti, zabave in blišča. Koncert godalnega kvarteta Al Fine naj služi kot glasbena voščilnica s poglobljeno refleksijo preteklosti ter upanjem na lepe trenutke v prihodnosti.

Vesele praznike!

Serenado za godala je Benjamin Ipavec skomponiral leta 1898. Z omenjenim delom je Ipavec postal eden vidnejših predstavnikov slovenske glasbe v drugi polovici 19. stoletja in tako je serenada še danes priljubljena, pogosto izvajana in globoko zasidrana v godalnem repertoarju.

Suita Hrestač ruskega glasbenega velikana Petra Iljiča Čajkovskega je nastala leta 1892. Skladatelj je suito uglasbil iz posameznih tem svojega istoimenskega baleta, ki ob prvi uprizoritvi žal ni požel uspeha. Balet je zasnovan po Hoffmanovi pripovedki Hrestač in Mišji kralj. Je dvodejanka, polna čarobnosti in upanja. Šele po skladateljevi smrti je balet s svojo božično vsebino postal del vsakoletnega prazničnega repertoarja številnih baletnih hiš širom po svetu.

V tretjem sklopu koncerta dovolimo, da nas ob glasbi C. Debussyja, G. Bregovića in E. Elgarja objamejo spomini. Njihova toplina (in grenkoba) sta nas oblikovala v to, kar mislimo, čutimo, verjamemo; v to, kar smo.

Zadnji del glasbenega večera bo zazvenel v sproščenem slogu in zabavnih ritmih. Praznični čas je tudi priložnost za druženje in zabavo. Naj vsak trenutek šteje! Carpe diem!

String Quartet Al Fine

Tonight's concert is dedicated to the spirit of the holiday season ahead. A time imbued with a touch of traditionality and enriched with the magic of expectation. A period of inner joy, memory and hope, as well as wit, fun and flash. The concert of the Al Fine String Quartet should serve as a music card with an in-depth reflection of the past and hope for beautiful moments in the future.

Happy holidays!

The Serenade for Strings was composed by Benjamin Ipavec in 1898. With this work, Ipavec became one of the most prominent representatives of Slovenian music in the second half of the 19th century, and thus the serenade is still popular, often performed and deeply anchored in a string repertoire.

The Nutcracker Suite of the Russian Music giant Peter Ilyich Tchaikovsky was created in 1892. The composer set the suite to music from the individual themes of his ballet of the same name, which unfortunately did not reap success at the time of its first performance. The ballet is based on Hoffman's tale The Nutcracker and the Mouse King. It is a two-part performance, full of magic and hope. It was only after the composer's death that the ballet, with its Christmas content, became part of the annual festive repertoire of numerous ballet houses around the world.

In the third part of the concert, we are allowed to be embraced by memories alongside the music of C. Debussy, G. Bregović and E. Elgar. Their warmth (and bitterness) shaped us into what we think, feel and believe - into who we are.

The last part of the musical evening will sound in a relaxed style with fun rhythms. The holiday season is also an opportunity to socialise and have fun. Make every moment count! Carpe diem!

Godalni kvartet Al Fine

Godalni kvartet Al Fine je nastal v letu 2017. Štirje akademski glasbeniki so se v zasedbo združili z željo, da s skupno igro in muziciranjem obarvajo dneve in širijo umetnost. Z nastopi na različnih prizoriščih ob raznovrstnih priložnostih želijo javnosti približati zasedbo godalnega kvarteta in številna dela, ki so bila napisana zanj. ´´Za vsako uho se glasba najde´´ je misel, ki jih spremlja in postavlja pred izziv. Želijo preseči idejo, da je glasba, ki jo izvajajo, rezervirana za ožjo publiko in koncertne dvorane. V koncertne programe poleg klasičnih del za godalni kvartet tako pogosto vključijo priredbe zabavne in popularne glasbe, ki pod njihovimi loki prepričljivo zazvenijo. Godalni kvartet Al Fine sestavljajo:

Violinistka **Urška Trček Lenarčič** je z odliko diplomirala na ljubljanski Akademiji za glasbo in vzporedno končala tudi študij muzikologije. Znanje in koncertne izkušnje je nabirala v mnogih komornih sestavih in orkestrih (klavirski trio, godalni kvartet in kvintet, Ljubljana International Orchestra, Orkester SF, Orkester RTV) ter nastopila na številnih koncertih in festivalih doma in v tujini (Festival Bled, Koncertni cikel Festine, festival St. John's Smith Square v Londonu...). Znanje in navdušenje prenaša na mlade glasbenike na Glasbeni šoli Vrhnika.

Violinistka **Petra Kravos** je diplomirala na Akademiji za glasbo v Ljubljani. V letih svojega izobraževanja se je udeleževala raznih mojstrskih tečajev in poletnih šol pri profesorjih, kot so Christiano Rossi, Marina Yashvilig, Paivyt Meller, Heilfried Fister, ... Svoje znanje in izkušnje je bogatila tudi na turnejah z orkestri Euro Young Classic, SFK Youth Symphony Orchestra, Animato in s sodelovanjem ter koncertiranjem z orkestroma RTV Slovenija in SNG Opera in balet Ljubljana. Sedaj poučuje na Glasbeni šoli Franca Šturma v Ljubljani, kjer z vso svojo vnemo deli svojim učencem znanje, izkušnje ter ljubezen do glasbe in violine.

Peter Kranjec, ki v kvartetu igra violo, je diplomiral iz violine na Akademiji za glasbo v Ljubljani in se po končanem študiju dve leti izpopolnjeval na Univerzi za upodabljajočo umetnost na Dunaju. Med študijem je aktivno sodeloval v različnih zasedbah in orkestrih ter se izpopolnjeval na glasbenih seminarjih doma in v tujini. Pridobljeno znanje posreduje učencem GŠ Franca Šturma v Ljubljani. Je predsednik Kulturnega društva Al Fine, ki od leta 2018 spodbuja zanimanje za glasbene dejavnosti in skupinsko muziciranje.

Violončelistka **Urša Kržič** je končala študij violončela na Akademiji za glasbo v Ljubljani. Kot članica klavirskega tria GUD je nastopila na številnih državnih in mednarodnih tekmovanjih in koncertnih prireditvah, se izpopolnjevala na priznani podiplomski šoli komorne igre Tria di Trieste ter za izjemne dosežke prejela študentsko Prešernovo nagrado AG. Sodelovala je tudi s komornim zborom Vokalna akademija Ljubljana, s katerim je osvojila veliko zborovsko nagrado Evrope. Svoje znanje predaja učencem GŠ Vrhnika, ki na državnih in mednarodnih tekmovanjih dosegajo najvišje uvrstitve v svojih kategorijah.

String Quartet Al Fine

In 2017 four academically trained musicians formed a string quartet and named it Al Fine – which in translation means "to the end". They believe there is music for every ear and that thought is guiding them when searching for repertoire and new projects. They have performed in several public concerts on various stages and occasions. Their repertoire is diverse, it ranges from classical to popular music. With arrangements of jazz standards and famous tunes and with concerts outside of concert halls (on streets, in parks, during weddings, at galleries and libraries) they promote chamber music by bringing it closer to people. Members of the String Quartet Al Fine are:

The violinist **Urška Trček Lenarčič** graduated from the Academy of Music in Ljubljana with a summa cum laude designation. She also studied musicology at the Faculty of Arts in Ljubljana. She has been a member of numerous orchestras, such as the Ljubljana International Orchestra and the Radio and Television Symphony Orchestra of Slovenia. She has appeared at many festivals in Slovenia and abroad, including the Bled Festival, the London Festival of Baroque Music and others. As a musician, she passes on her musical knowledge to younger generations as well; she is a teacher at music schools in Vrhnika.

The violinist **Petra Kravos** graduated from the Academy of Music in Ljubljana. During her studies, she improved her knowledge at many masterclasses held by renowned professors such as Christiano Rossi, Marina Yashvilig, Paivyt Meller, Heilfried Fister,... She gained knowledge and experience through concert performances on international stages as a member of chamber groups and orchestras such as Euro Young Classic, SFK Youth Symphony Orchestra, Animato and with our national orchestras, the Symphony Orchestra RTV Slovenija and SNG Opera and Ballet Ljubljana. She currently works as a teacher at Franc Šturm Music School in Ljubljana, where she is passing her knowledge and love for music and violin to her students with all her passion and enthusiasm.

After graduating in violin from the Academy of Music in Ljubljana, the violist **Peter Kranjec** enhanced his musical skills at the University of Music and Performing Arts in Vienna. During his studies, he was a member of various ensembles and orchestras. He also perfected his musical knowledge and performing skills at masterclasses in Slovenia and abroad. He passes his knowledge on to children at the Franc Šturm Music School in Ljubljana. As the president of the cultural society Kulturno društvo Al Fine, he promotes chamber music from sociological, psychological and musical points of view.

The cellist **Urša Kržič** graduated from the Academy of Music in Ljubljana as well and specialised in chamber music at the prestigious postgraduate chamber music school Tria di Trieste in Italy. For her outstanding achievements in chamber music, she was awarded the Prešeren award of the Academy of Music in Ljubljana. She is currently a teacher at the Music School Vrhnika; her students are being awarded the highest awards at national and international music competitions.

Kazalo / Contents